Radiation therapy at compact Compton sources

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ABSTRACT

The principle of the compact Compton source is presented briefly. In collision with an ultrarelativistic electron bunch a laser pulse is back-scattered as hard X-rays. The radiation cone has an opening of a few mrad, and the energy bandwidth is a few percent. The electrons that have an energy of the order of a few tens of MeV either circulate in storage ring, or are injected to a linac at a frequency of 10–100 MHz. At the interaction point the electron bunch collides with the laser pulse that has been amplified in a Fabry-Perot resonator. There are several machines in design or construction phase, and projected fluxes are 10^{12} to 10^{14} photons/s. The flux available at 80 keV from the ThomX machine is compared with that used in the Stereotactic Synchrotron Radiation Therapy clinical trials. It is concluded that ThomX has the potential of serving as the radiation source in future radiation therapy programs, and that ThomX can be integrated in hospital environment.

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Introduction

The use of synchrotron radiation (SR) has opened new avenues in biomedical research [1,2]. 3-dimensional structures of macroscopic objects can be imaged with a resolution of a few microns and elemental distributions in cells can be mapped with spatial resolution better than 100 nm. These are made possible by the high intensity and natural collimation, energy tunability, and partial transverse coherence of SR, which are utilized in phase contrast imaging and in X-ray micro-spectroscopy.

The limited availability of SR has curtailed the applications mostly to basic research, and to methods development with the distant goal of clinical use. Only a few programs have reached the stage of human studies, the first being coronary angiography with intravenous injection of the Iodine contrast agent. For these studies a new method, K-edge subtraction (KES) imaging was developed, and has been applied in studies of circulation and ventilation in animal models. The radiation dose in KES imaging is within clinically acceptable limits, and there are many potential applications in functional imaging of human organs [3]. Phase contrast imaging in the propagation mode has been used in mammography, demonstrating enhanced contrast resolution [4]. Clinical trials for radiation therapy of brain tumors is underway at the European

Synchrotron Radiation Facility (ESRF) using the Stereotactic Synchrotron Radiation Therapy (SSRT) method [5].

There have been many projects for transfer of phase contrast imaging methods to clinical environment without the use of large scale synchrotrons see Ref. [2]. In most cases, rotating anode or micro-focus X-ray tubes are used as radiation sources, and new concepts have been introduced to overcome the anode cooling problems. The anode may be replaced by a wire or thin stream of liquid metal, and potentially these sources are at least an order of magnitude brighter than conventional X-ray tubes. However, even with these improvements the exposure times would be prohibitively long for most modalities of human imaging.

Probably the only way to break out of the confinement of scarce synchrotron radiation at large facilities on one hand, and the insufficient X-ray flux from tube sources on the other, is the introduction of compact SR sources for dedicated medical imaging and/or therapy facilities. Most concepts of compact sources are based on the use of very high-field magnets in small storage rings, but still the X-ray energies remain too low for most imaging applications, and totally exclude radiation therapy [6]. A different way of producing X-rays from a high-energy electron beam is to collide the beam with a laser beam, which is scattered back in a process that is usually called inverse Compton scattering [7]. Originally, the method was introduced in high-energy particle physics, but more than a decade ago it was demonstrated that a linac-laser combination produces short, intense X-ray pulses of sufficient intensity for medical imaging [8]. In recent years, many projects have been

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initiated, and the first and the only compact inverse-Compton source on market is the Lynceantech machine, which delivers X-rays in the range 15–35 keV [9]. It is expected that these sources will become standard equipment for clinical imaging in large hospitals.

Inverse Compton scattering and compact Compton sources

The inverse Compton scattering process is shown schematically in Fig. 1(a). In the collision, the energy of the electron is transmitted to the photon. The kinematics of the process can be described as collision of two particles, or using the synchrotron radiation analogy, where the electron travels through the “micro-undulator” of the electromagnetic field of the photon. The energy of the scattered photon in the laboratory frame is [10]:

$$E_X = 2\gamma^2 E_L (1 + \cos\theta_c) / (1 + \gamma^2 \theta^2), \quad (1)$$

where γ is the electron energy in the units of its rest energy, $\gamma = E_e/mc^2$, E_L the energy of the incoming photon, θ_c and θ respectively the incident angle and the scattering angle with respect to the electron trajectory. In derivation of (1), it is assumed that $\gamma \gg 1$ and $E_L \ll mc^2$. Expression (1) shows that there is an univocal relation between the energy and the emission angle of Compton photons, the hardest radiation being concentrated on-axis where $\theta = 0$. So in head-on collision (i.e. when $\theta_c = 0$), the maximum energy of the scattered photons is $E_X^{\max} = 4\gamma^2 E_L$. For instance, 0.1 nm (12.4 keV) X-rays are produced in collision of a laser pulse of 1.0 μm wavelength ($E_L = 1.24$ eV) with a 25 MeV electron bunch. The normalized spectral cross section $\sigma_\omega(\omega)$, where $\omega = E_X/E_X^{\max}$, is represented on Fig. 1(b) and can be written as [11]:

$$\sigma(\omega) = 3/2 (1 - 2\omega + 2\omega^2). \quad (2)$$

For electron/laser collisions in the x–z plane, the number of X-rays emitted per second is:

$$F_{\text{tot}} = \frac{\sigma_T N_e N_L f_{\text{rep}} \cos(\theta_c/2)}{2\pi \sqrt{\sigma_{ye}^2 + \sigma_{yL}^2} \sqrt{\sigma_{xe}^2 + \sigma_{xL}^2 + \sin^2(\theta_c/2) (\sigma_{ze}^2 + \sigma_{zL}^2)}} \quad (3)$$

where σ_T is the Thomson cross-section, N_e the number of electrons per bunch, N_L that of photons per laser pulse, and f_{rep} the repetition rate of collisions. The transverse and longitudinal sizes of the (Gaussian) electron bunches and laser pulses at the interaction point are given by $\sigma_{xe,ye} = \sigma_e$, $\sigma_{xL,yL} = \sigma_L$, σ_{ze} and σ_{zL} respectively. The charge of an electron bunch may be 0.1–1.0 nC, so N_e is about 10^9 , and the repetition rate is between 10^7 1/s and 10^8 1/s. To give a concrete example with feasible values of $f_{\text{rep}} = 20$ MHz, 1 nC electron bunches, and 10 mJ laser pulses of 1 μm wavelength, $F \sim 10^{13}$ ph/s is expected when $\sigma_e = \sigma_L = 40$ μm .

Figure 1. Inverse Compton scattering process (a) and normalized Compton cross section as a function of $\omega = E_X/E_X^{\max}$ (b).

There are basically two machine designs: the storage ring scheme and the linac scheme, illustrated in Fig. 2. Each one has advantages and technical difficulties. In the storage ring scheme each stored electron bunch interacts many times with a laser pulse. The bunch is blurred by intra-beam scattering and Compton scattering, so that it is ejected and replaced by a new bunch. The repetition frequency is determined by the ring circumference, for instance f_{rep} is 20 MHz when the circumference of 15 m. In the linac scheme each electron bunch interacts only once, and f_{rep} is determined by the electron gun, which is necessarily a superconducting device. The advantage of the linac scheme is the small transverse size of the electron bunch, so that the transverse coherence of the X-ray beam is high. However, continuous cryogenic operation of the electron gun with high repetition rate entails many technical and operational challenges, particularly in clinical environment. In both schemes, intense laser pulses at frequency f_{rep} are created by the amplification of pulses from a low average power pulsed laser which are then sent in a high gain optical resonator for a second amplification stage. For instance, a 10 mJ laser pulse circulating at 20 MHz frequency corresponds to 0.2 MW stored in the optical cavity.

The properties of the X-ray beam depend on the energy spreads of the electron and laser beams, $d\gamma$ and dE_L , respectively, and on the divergences of the beams. The relative bandwidth of on-axis photons due to energy spreads of the beams is approximately $dE_L/E_L + 2d\gamma/\gamma$, which is typically of the order of 10^{-3} . More important are the effects of beam divergences, and the dominant factor is the electron beam divergence $\sigma'_{xe,ye} = \sigma'_e$, yielding $dE_X/E_X = 2(\gamma\sigma'_e)^2$. With typical values of $\gamma = 100$ (50 MeV electron beam) and $\sigma'_e = 1$ mrad, the relative energy spread of the X-ray beam is 2%.

The brilliance B of the source is given as the number of X-ray photons per second, per mm^2 of source, in solid angle of 1 mrad^2 , and in 0.1% spectral bandwidth. Considering only the dominant term due to the electron beam divergence, on-axis B is proportional to $F\gamma^2/\epsilon_N$, where $\epsilon_N = \gamma\sigma_e\sigma'_e$ is the normalized (transverse) emittance of the electron beam [10]. In the same way as for the degree of transverse coherence, the electron beam emittance is the crucial factor for the X-ray beam brilliance.

Figure 2. Basic schemes of high-flux compact Compton sources. IP is the interaction point of the laser pulse with the electron bunch.

Compact Compton source projects

For biomedical applications, the compact source intensity (ph/s/mrad²) should be comparable to the intensity of monochromated bending magnet radiation of synchrotron sources, i.e. 10¹¹–10¹² ph/s/mrad². In addition to the existing Lynceantech machine, several sources of higher intensity and higher X-ray energies are being designed [10]. Some characteristics and orders of magnitude of these are collected in Table 1.

The superconducting linac-based machines provide the highest brilliance but still face many technical challenges and will require extensive radiation shielding. For many medical imaging methods and for radiation therapy in particular the brilliance is not critical, but more important is the flux available in a given solid angle. Therefore, one of the storage-ring machines in advanced design/construction phase is taken as a concrete example. The essential parameters of the ThomX machine [12] are given in Table 2.

Selecting a part of a Compton beam with a diaphragm of half angular aperture θ_{mr} of a few mrad, the flux of photons $F_{\theta_{\text{mr}}}$ contained in this radiation cone and the energy bandwidth can be written with a good approximation as:

$$F_{\theta_{\text{mr}}} = F_{\text{tot}} (\gamma^2 \theta_{\text{mr}}^2) \sigma(\omega_{\text{mr}}), \quad (4)$$

$$dE_X/E_X \sim \sqrt{(\gamma^2 \theta_{\text{mr}}^2)^2 + (2\gamma^2 \sigma_e'^2)^2 + (2d\gamma)^2}, \quad (5)$$

where $\omega_{\text{mr}} = 1 - (\gamma \theta_{\text{mr}})^2$. The first term in (5) is due to the univocal energy/angle relation (1), the two last terms are due to the divergence and the energy spread of the electron beam respectively. Results of calculation using parameters of Table 2 with a value of 67 MeV for the electron beam energy are shown in Fig. 3. The total flux and the flux in different opening angles of radiation cone are shown as a function of σ_e and σ_e' (top) and as a function of the X-ray energy bandwidth (bottom). According to (1), (3), (4) and (5), fluxes decrease as σ_e increases, the energy bandwidth increases with the opening angle θ_{mr} and with the divergence σ_e' of the electron beam. These plots are used for assessment of the suitability of ThomX for radiation therapy.

Stereotactic Synchrotron Radiation Therapy (SSRT)

The only synchrotron radiation therapy program that has reached the stage of human studies is the Stereotactic Synchrotron Radiation Therapy at the ESRF. The technical parameters and the protocol have been optimized for treatment of brain tumors, which have been “loaded” by an Iodine compound for radiation dose enhancement. As a compromise between beam penetration through the skull and excitement of Iodine fluorescence and secondary electrons, 80 keV incident radiation is used. The beam from

Table 1

X-ray compact Compton source projects aiming to produce a flux larger than 10¹² ph/s [10]. SR and Linac mean Storage Ring and Linac schemes, respectively, and (sc) indicates the projects using superconducting technologies. σ_s is the transverse source size.

Project	Type	E_X (keV)	ph/s	ph/s/mrad ²	σ_s (μm)
TTX	SR	20–80	10 ¹²	6.10 ⁹ –2.10 ¹⁰	50
LEXG	SR (sc)	33	10 ¹³	10 ¹¹	20
NESTOR	SR	30–500	10 ¹³	10 ¹¹ –10 ¹²	70
ThomX	SR	20–90	10 ¹³	6.10 ¹⁰ –3.10 ¹¹	70
KEK QB	Linac (sc)	35	10 ¹³	10 ¹¹	10
KEK ERL	Linac (sc)	67	10 ¹³	2.10 ¹¹	30
MIT	Linac (sc)	3–30	10 ¹⁴	10 ¹¹ –10 ¹²	2

Table 2

Nominal collision parameters of the ThomX project. ϵ_N and $d\gamma$ are the mean of the emittance and energy spread on one fill of 20 ms.

ThomX nominal parameters		
Interaction angle (θ_c)	2	Degree
Repetition rate (f_{rep})	17.8	MHz
Injection frequency	50	Hz
Electron energy	50–70	MeV
Electron bunch charge	1	nC
Electron normalized emittance (ϵ_N)	10	mm.mrad
Electron energy spread ($d\gamma$)	0.35	%
Laser wavelength	1.03	μm
Laser pulse energy	30	mJ
Laser pulse transverse size (σ_L)	40	μm

Figure 3. X-ray flux to different opening angles of the radiation cone as a function of σ_e and σ_e' (top) and as a function of the X-ray energy bandwidth (bottom). The electron energy is 67 MeV, and the average normalized emittance during a 20 ms fill of the storage ring is $\epsilon_N = 10$ mm.mrad. Total flux (black), fluxes in 0.5 mrad (purple), 1 mrad (red), 1.5 mrad (blue) and 2 mrad (green). (For interpretation of the references to color in this figure caption, the reader is referred to the web version of this article.)

a multipole wiggler is filtered by carbon, aluminum, and copper foils to remove soft radiation and reduce the heat load on the optical elements of the beamline. About 0.1% (80 eV) energy band is separated by a bent-crystal, double-Laue monochromator [13]. Typically, the beam height is 2 mm, and the maximum width is 150 mm. The measured skin entry dose rate is 0.5 Gy/s, when the storage ring current is 200 mA. This corresponds to 1.6×10^{10} ph/s/m² of 80 keV photons.

In the treatment the dose is averaged by moving the patient vertically. The radiation treatment set-up is shown in Fig. 4. The exposed area is defined by a hole in mask, which corresponds to the tumor area seen from that direction. The tumor is imaged at the hospital with a CT scanner, and the location and tumor dimensions are verified by CT imaging at the beamline. If the height of the beam is 2.0 mm, and the vertical opening of the mask 30 mm, the average dose rate is 35 mGy/s. This corresponds to

Figure 4. The SSRT clinical trials set-up at ID17 of the ESRF. The incident beam (top, right) passes through an aperture that corresponds to the tumor cross-section.

about 1.1×10^9 ph/s/mm². At the typical tumor location the absorbed dose is reduced to about 0.5 Gy/min. The total dose at the tumor depends on the number of irradiation ports (maximum 10), and the speed of the vertical scan. For safety reasons and for regulation of the dose, many fast scans are performed instead of one slow scan. The absorbed dose at the tumor is proportional to the total irradiation time, for instance 10 Gy is delivered in 20 min.

There is a wide margin for increase of the dose. ID17 has two wigglers of approximately equal radiation powers, and the height of the monochromatic beam can be doubled. In addition, the dose enhancement at the tumor may be substantially increased by the use of a more concentrated Iodine solution in the tumor circulation. The clinical trials are in Phase II at the moment, with 7 patients treated so far, and in the forthcoming trials therapeutic doses (several tens of Gy) will be used.

SSRT with ThomX

The above analysis of the SSRT clinical trials gives guidelines and benchmarks for the potential use of ThomX in radiation therapy. In the following calculations the value of 67 MeV for the electron beam energy is assumed. According to (1), this leads to 80.5 keV on-axis X-rays.

It is inferred from Fig. 3 that ThomX could provide an X-ray flux from 1.9×10^{12} to 4.1×10^{10} in a cone of 1.5 mrad half opening angle depending on the values of the transverse size and the divergence of the electron beam (blue curve on the top figure). Figure 3 shows also the bandwidth in that 1.5 mrad cone (blue curve on the bottom figure): for instance 0.88×10^{12} ph/s in 5% bandwidth should be available ($\sigma_e = 80 \mu\text{m}$ and $\sigma'_e = 0.94$ mrad in this case) and 1.5×10^{12} ph/s in 10% bandwidth (if $\sigma_e = 47 \mu\text{m}$ and $\sigma'_e = 1.6$ mrad). Through a mask opening of 30 mm diameter placed at 10 m from the ThomX interaction point, the corresponding intensities are about 1.25×10^9 ph/s/mm² and 2.1×10^9 ph/s/mm² respectively. These values are very close to the average intensity in the present SSRT clinical trials at the ESRF. If required, the absorbed dose at the tumor may be increased by a more concentrated Iodine solution and by decreasing to distance of the patient from the X-ray source; 10 m used in the above calculations is actually a rather conservative estimate. A schematic layout of the ThomX machine for radiation therapy is shown in Fig. 5.

The design parameters of ThomX are based on existing and proven technical solutions. The storage ring scheme is easily adapted to hospital environment. The fill frequency is only 50 Hz, so the energy stored in the electron beam is a few watts only, and little radiation shielding is required. In addition, the machine could be routinely operated by non-expert staff provided that simple control tools are developed and integrated. The most critical component is probably the Fabry-Perot resonator, which must be well isolated from all sources of vibrations. On the other hand, superconducting machines may be more difficult to integrate and operate because of the requirement of an extensive radiation shielding and the complications related to cryogenic systems. The electron gun operates at 10–100 MHz injection frequency leading to a stored energy of several tens of kilowatts.

Conclusions

The comparison of the X-ray intensity available from ThomX with the average intensity in the ongoing clinical trials of SSRT at the ESRF demonstrates the feasibility of radiation therapy with a compact Compton source (CCS). A CCS based on the storage ring scheme is compatible with clinical environment, and the CCS can be used also for medical imaging modalities that have been developed at synchrotron radiation facilities.

Figure 5. The layout of ThomX.

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